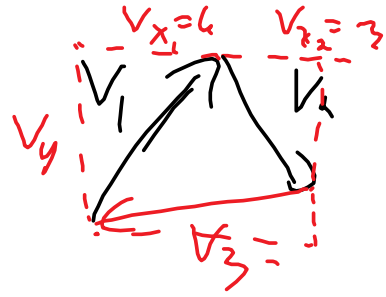


$$V_1 = \begin{pmatrix} x, y, z \\ 6, 0, 8 \end{pmatrix}$$

$$V_2 = \begin{pmatrix} 3, 4, -3 \end{pmatrix}$$

$$V_3 = \begin{pmatrix} -9, -4, -5 \end{pmatrix}$$



$$b) V_1 = (6, 0, 8)$$

$$-V_2 = (-3, -4, +3)$$

$$V_3 = (-3, +4, -11)$$

Q17

$$V_y = ? \sqrt{86.6^2 - 35.4^2}$$

$$= \boxed{79.0}$$

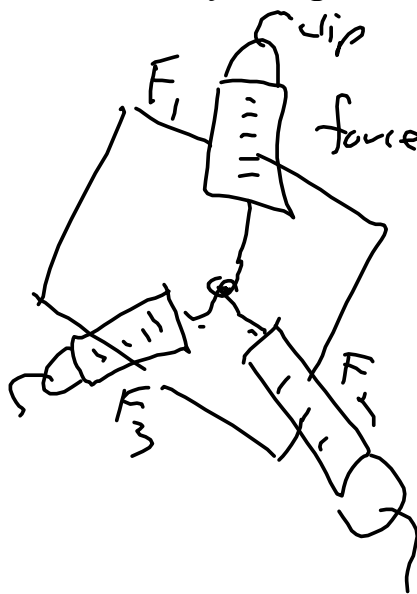
$$\theta = \cos^{-1} \left(\frac{35.4}{86.6} \right) = \boxed{65.8^\circ}$$

to the x-axis

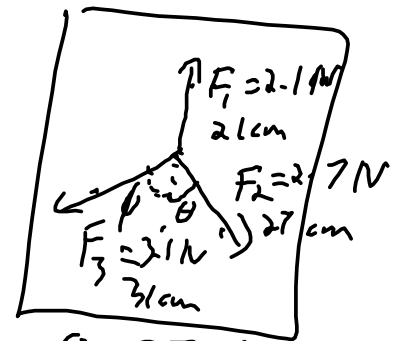
Lab - not formal - no report

Hand in:

1. Free body diagram of the 3 forces.



scale $1N = 10cm$



$$\theta = 37.1^\circ$$

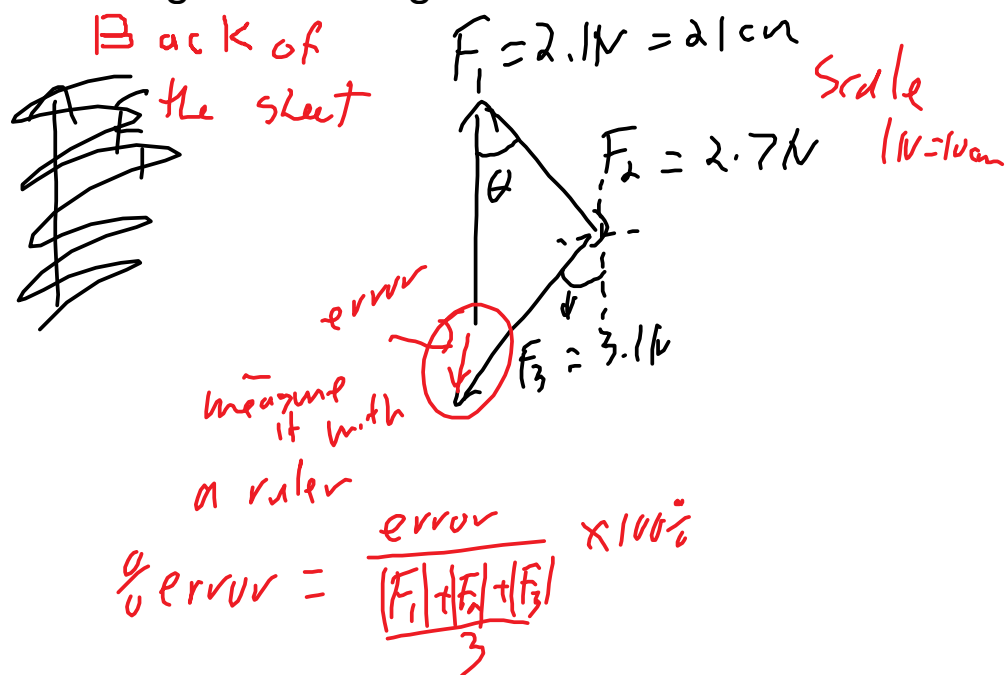
$$\phi = 42.7^\circ$$

Free body diagram
- shows forces

2. Convert the free body diagram into a vector addition diagram.

Draw F_1 in the same direction but draw F_2 head to tail with F_1 , then draw F_3 head to tail.

The space remaining on the diagram is the error.



3. Calculate the components of each vector and the sum of the components = error.

F1 should have no x component, only y.

$$F_{2x} = F_2 \sin \theta$$

$$F_{2y} = -F_2 \cos \theta$$

$$F_{3x} = -F_3 \sin \phi$$

$$F_{3y} = -F_3 \cos \phi$$

all good?

$$F_x = F_{1x} + F_{2x} + F_{3x}$$

$$F_y = F_{1y} + F_{2y} + F_{3y}$$

$$\text{error} = \sqrt{F_x^2 + F_y^2}$$

Quiz answers version 1

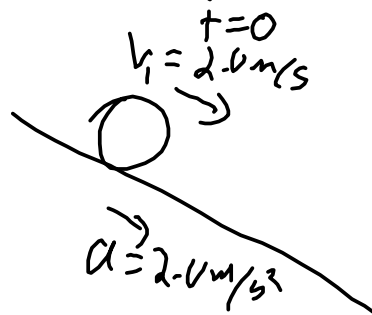
1a) $1.783 \times 3.45 = 6.1514 = 3 \text{ sig figs } 6.15 \text{ m}^2$

b) $0.00056 + 0.06001 = 0.06057 \text{ kg}$

c) $5.5014 \times 1.90 = 10.4527 \times 10^5 = 1.05 \times 10^6 \text{ s}^2$

$$\begin{array}{r} 11.5004 \text{ ms} \\ 990 \text{ ms} \\ \hline 11.4004 \text{ ms} \end{array} \quad \boxed{11.40 \text{ ms}}$$

Q2 a)



a) $v_i = 2.0 \text{ m/s}$
 $t = 2.0 \text{ s}$
 $a = 2.0 \text{ m/s}^2$
 $v_f = ?$

$$\begin{aligned} v_f &= v_i + at \\ &= 2.0 \text{ m/s} + 2.0 \text{ m/s}^2 (2 \text{ s}) \\ &= \boxed{6.0 \text{ m/s}} \end{aligned}$$

b) $d = 20 \text{ m}$
 $t = ?$
 $a = 2.0 \text{ m/s}^2$

$$d = \frac{1}{2} at^2 + v_i t$$

$$v_i = 2.0 \text{ m/s}$$

$$2v = t^2 + 2t$$

$$0 = t^2 + 2t - 20 \quad \leftarrow 9.165$$

$$t = \frac{-2 \pm \sqrt{4 - 4(-20)}}{2}$$

$$v_f^2 = v_i^2 + 2ad$$

$$v_f = at + v_i$$

$$t = 3.585 \quad \Rightarrow \quad t = 3.6 \text{ s}$$

c) $d = d$

$$10 \text{ m/s}(t-1) = \frac{1}{2}(2 \text{ m/s}^2)t^2 + 2 \text{ m/s} t$$

$$10t - 10 = t^2 + 2t$$

$$0 = t^2 - 8t + 10$$

$$\frac{8 \pm \sqrt{64 - 4(10)}}{2} \quad \leftarrow 4.89$$

$$\frac{8 - 4.89}{2} = 1.5505 \text{ s}$$

$$v=0 \quad d = 10 \text{ m/s}(1.5505 \text{ s} - 1 \text{ s}) = \boxed{5.5 \text{ m}}$$

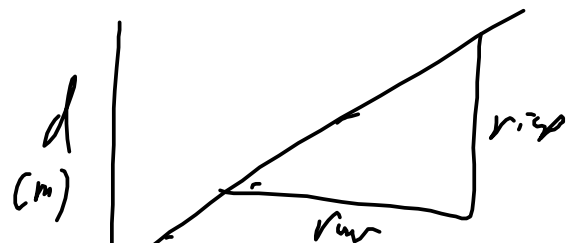
d) $\begin{matrix} \uparrow \\ 2.9 \text{ m} \\ \downarrow \end{matrix} \quad t = ?$

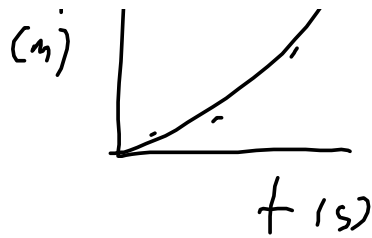
$$d = \frac{1}{2}at^2$$

$$t = 0.77 \text{ s} \times 2 = \boxed{1.5 \text{ s}}$$

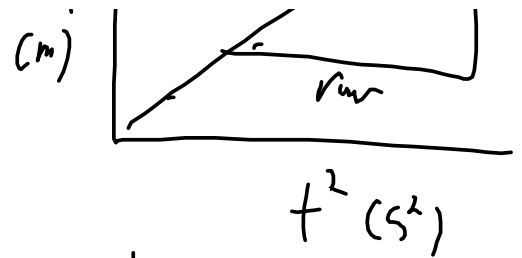


$\frac{1}{1}$





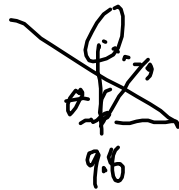
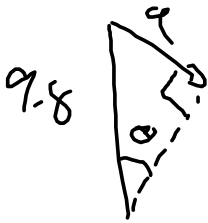
$$d = \frac{1}{2} a t^2$$



Slope = 4.0 m/s^2

equation $d = 4.0 \text{ m/s}^2 t^2$

Bonus: $a = 2 \times \text{slope} = 8.0 \text{ m/s}^2$



$$a = g \sin \theta$$

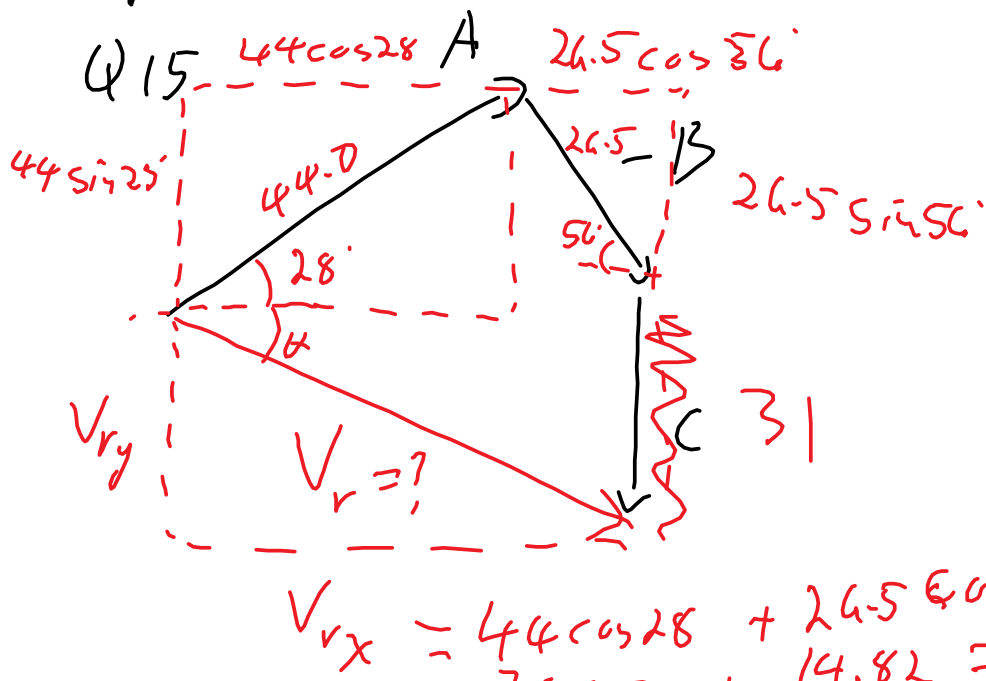
$$\theta = \sin^{-1} \frac{8}{9.6} = 54.7^\circ$$

Lab - 2 diagrams and components

Labbook q 1-5 p38-39

Answers are at the back, but show your work

P61



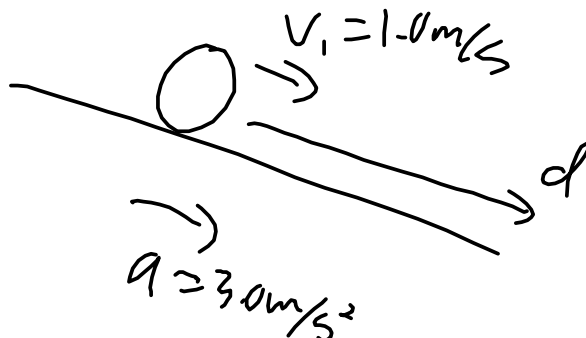
$$\begin{aligned}
 V_{rx} &= 44 \cos 28 + 26.5 \cos 56 \\
 &= 38.85 + 14.82 = 53.67 \\
 V_{ry} &= 44 \sin 28 + 26.5 \sin 56 + 31 \\
 &= 20.66 + 21.97 + 31 = 73.63 \\
 V &= \sqrt{V_{rx}^2 + V_{ry}^2} = \sqrt{53.67^2 + 73.63^2} = 91.63 \\
 \phi &= \tan^{-1} \frac{53.67}{73.63} = 36.31^\circ \\
 \theta &= 90^\circ - \phi = 53.69^\circ
 \end{aligned}$$

Quiz version 2

- 1a) $2.783 \times 3.45 = 9.6014 = 9.60 \text{ m}^2$
 b) $0.00026 + 0.06001 = 0.06027 \text{ kg}$
 c) $5.2014 \times 1.90 = 9.8827 = 9.88 \times 10^5 \text{ s}^2$

$$\begin{array}{r}
 1.2004 \text{ ms} \\
 9.90 \text{ ms} \\
 \hline
 11.1004 \text{ ms}
 \end{array}$$

$$\boxed{11.10 \text{ ms}}$$



$$\begin{aligned}
 a) \quad V_f &= V_i + at \\
 V_f &= 1.0 \text{ m/s} + 3.0 \text{ m/s}^2 \times 2.0 \text{ s} \\
 &= 7.0 \text{ m/s}
 \end{aligned}$$

$$b) \quad V_f^2 = V_i^2 + 2ad$$

$$V_f^2 = 1^2 + 2(3)(20)$$

$$V_f = \sqrt{121} = 11 \text{ m/s}$$

$$V_f = V_i + at \quad 11 = 1 + 3t$$

$$\boxed{t = 3.3 \text{ s}}$$

c) $d = d$

$$10 \text{ m/s} (t-1) = \frac{1}{2} at^2 + V_i t$$

$$10t - 10 = 1.5t^2 + t$$

$$0 = 1.5t^2 - 9t + 10$$

$$\frac{9 \pm \sqrt{81 - 4(1.5)10}}{2(1.5)} = \frac{9 \pm \sqrt{21}}{3}$$

$$t = 1.47 \text{ s}$$

$$d = Vt = 10 \text{ m/s} (1.47 \text{ s} - 1)$$

$$\boxed{4.7 \text{ m}}$$

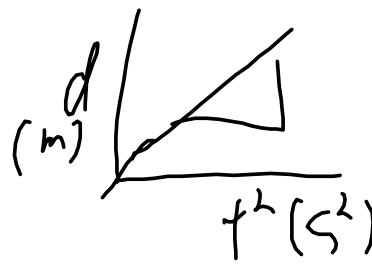
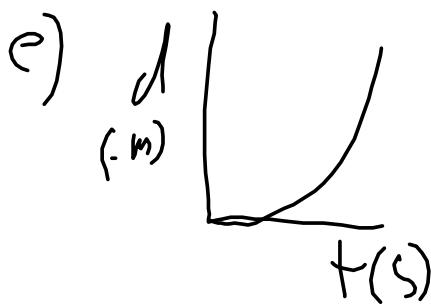
$$\boxed{35.2 \text{ m}}$$

d) $d = 2.9 \text{ m}$

$$V_i = 0$$

$$d = \frac{1}{2} at^2$$

$$t = \sqrt{\frac{2(2.9)}{9.8}} = 0.77 \text{ s} \times 2 = \boxed{1.5 \text{ s}}$$



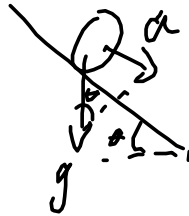
$$\text{slope} = 4.0 \text{ m/s}^2$$

$$d = 4.0 \text{ m/s}^2 t^2$$

$$d = \left(\frac{1}{2} a\right) t^2$$

$$a = 8 \text{ m/s}^2$$

Bonus:



$$\sin \theta = \frac{a}{g}$$

$$\theta = \sin^{-1} \frac{8}{9.8}$$

$$\boxed{\theta = 54.7^\circ}$$

Lab

scale free body diagram - force determines the length of the vector

scale vector addition diagram

components

Q1-5 p38-39 labbook - answers at the back

Quiz version 3

1a) $7.183 \times 4.45 = 31.9644 = 32.0 \text{ m}^2$
 3sf 3sf

b) $0.0076 + 0.07001 = 0.07761 = 0.0776 \text{ kg}$
 to the 4th digit

c) $5.714 \times 2.90 = 16.5706 = 1.66 \times 10^6 \text{ s}^2$

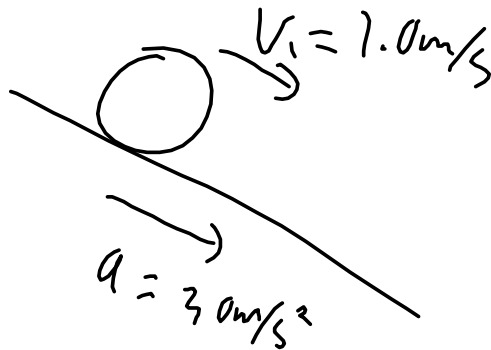
$$\begin{array}{r} 7.004 \text{ ms} \\ + 9.70 \text{ ms} \\ \hline 16.704 \text{ ms} \end{array}$$

$$\boxed{16.70 \text{ ms}}$$

$$\begin{array}{r}
 7.004 \text{ ms} \\
 + 9.70 \text{ ms} \\
 \hline
 11.4004
 \end{array}$$

$$11.40 \text{ ms}$$

Q2



a) $V_f = ?$
 $t = 2.0 \text{ s}$

$$V_f = V_i + at$$

$$\begin{aligned}
 V_f &= 1.0 \text{ m/s} + 3.0 \text{ m/s}^2 (2.0 \text{ s}) \\
 &= 7.0 \text{ m/s}
 \end{aligned}$$

b) $d = 20 \text{ m}$

$$V_f^2 = V_i^2 + 2ad$$

$$V_f^2 = (1 \text{ m/s})^2 + 2(3 \text{ m/s}^2)(20 \text{ m})$$

$$V_f^2 = 1 \text{ m}^2/\text{s}^2 + 120 \text{ m}^2/\text{s}^2$$

$$V_f = \sqrt{121 \text{ m}^2/\text{s}^2} = 11.0 \text{ m/s}$$

$$\begin{aligned}
 V_f &= V_i + at & t &= \frac{V_f - V_i}{a} = \frac{11.0 \text{ m/s} - 1.0 \text{ m/s}}{3.0 \text{ m/s}^2} \\
 & & &= 3.3 \text{ s}
 \end{aligned}$$

e) $d_{\text{yon}} = d_{\text{close}}$

$$V(t-1) = \frac{1}{2}at^2 + v_i t$$

$$10t - 10 = 1.5t^2 + t$$

$$0 = 1.5t^2 - 9t + 10$$

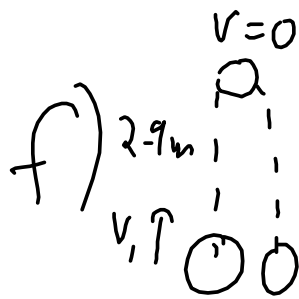
$$\frac{9 \pm \sqrt{81 - 4(1.5)10}}{2(1.5)} = \frac{9 \pm \sqrt{21}}{3}$$

4.583
↓

$$\approx 1.47s$$

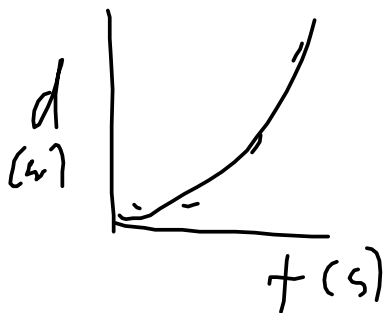
$$d = V(t-1) = 10m/s (1.47s - 1.0s)$$

$$= \boxed{4.7m}$$



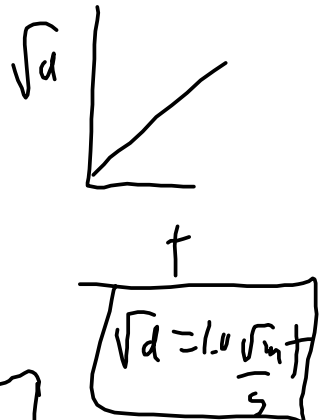
$$d = \frac{1}{2}at^2$$

$$t = \sqrt{\frac{2(2.9)}{9.8}} = 0.769 \times 2 = \boxed{1.5s}$$



$$m = 1.0m/s^2$$

$$\boxed{d = 1.0m/s^2 t^2}$$

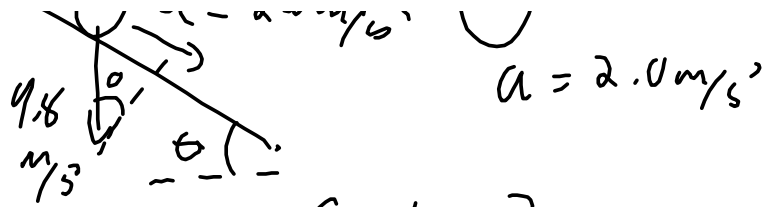


Bonus:

$$a = 2.0m/s^2$$

$$d = \left(\frac{1}{2}at^2\right)$$

$$a = 2.0m/s^2$$



$$\sin \theta = \frac{2}{9.8}$$

$$\boxed{\theta = 11.8^\circ}$$